



# QuantumNAT: Quantum Noise-Aware Training with Noise Injection, Quantization and Normalization

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# Outline

- Overview
- Background
- QuantumNAT Methodology
- Evaluation
- TorchQuantum Library
- Conclusion

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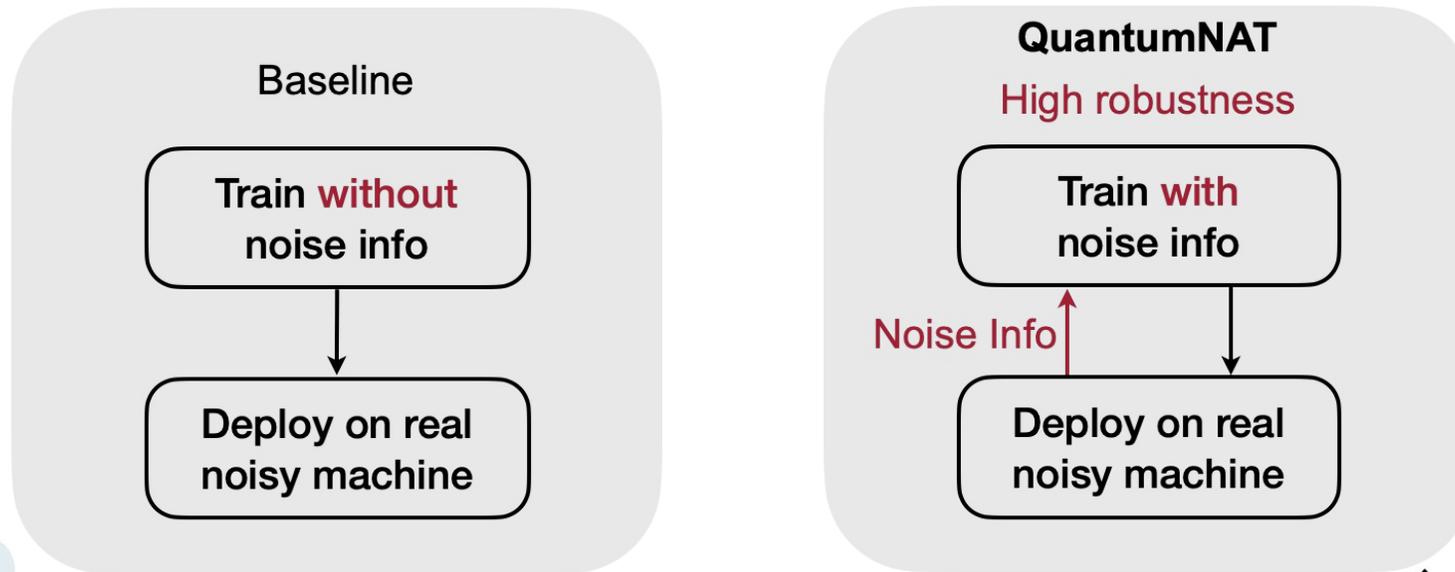
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# Overview: Noise-Aware Training

- Quantum circuits are noisy
  - Noise severely **degrades** the circuit performance

# Overview: Noise-Aware Training

- Quantum circuits are noisy
  - Noise severely **degrades** the circuit performance
- Add real device noise during circuit training on classical simulator
  - Improve robustness on real quantum machines

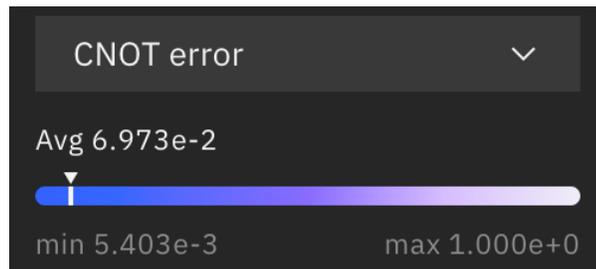
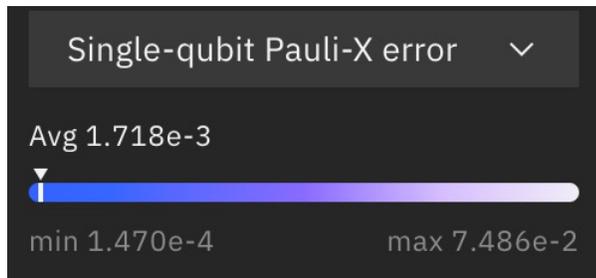


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# NISQ Era

- Noisy Intermediate-Scale Quantum (NISQ)
  - **Noisy**: qubits are sensitive to environment; quantum gates are unreliable

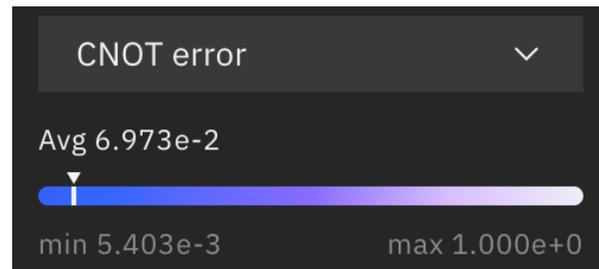
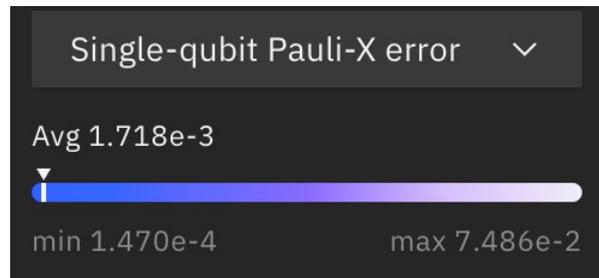


Gate Error Rate

<https://quantum-computing.ibm.com/>

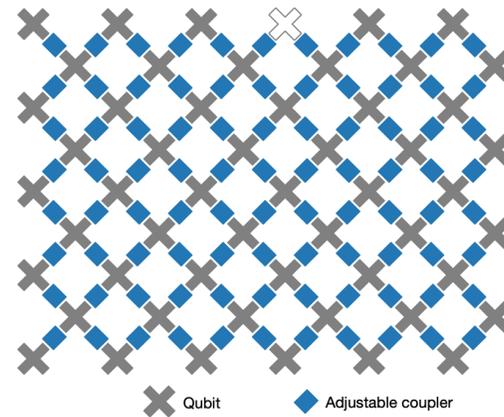
# NISQ Era

- Noisy Intermediate-Scale Quantum (NISQ)
  - **Noisy**: qubits are sensitive to environment; quantum gates are unreliable
  - **Limited number** of qubits: tens to hundreds of qubits



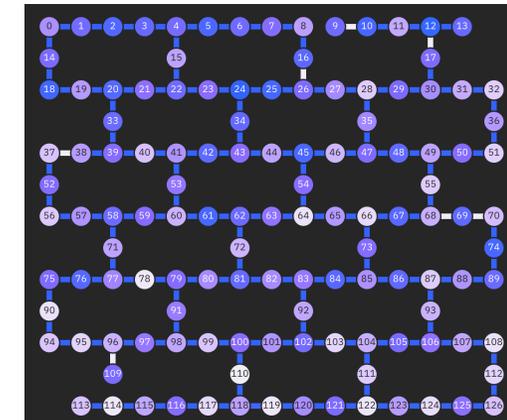
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Google Sycamore

<https://www.nature.com/articles/s41586-019-1666-5>

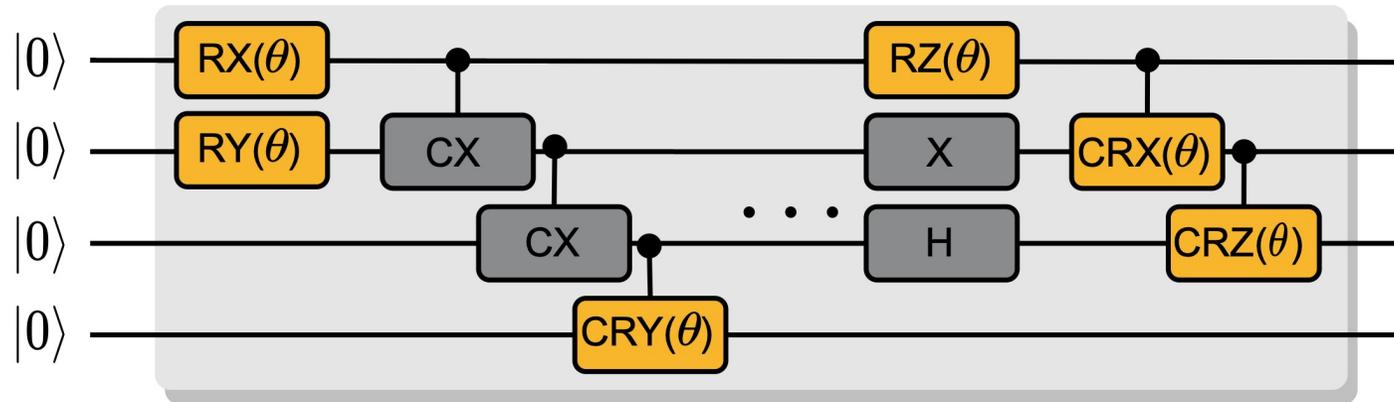


IBM Washington

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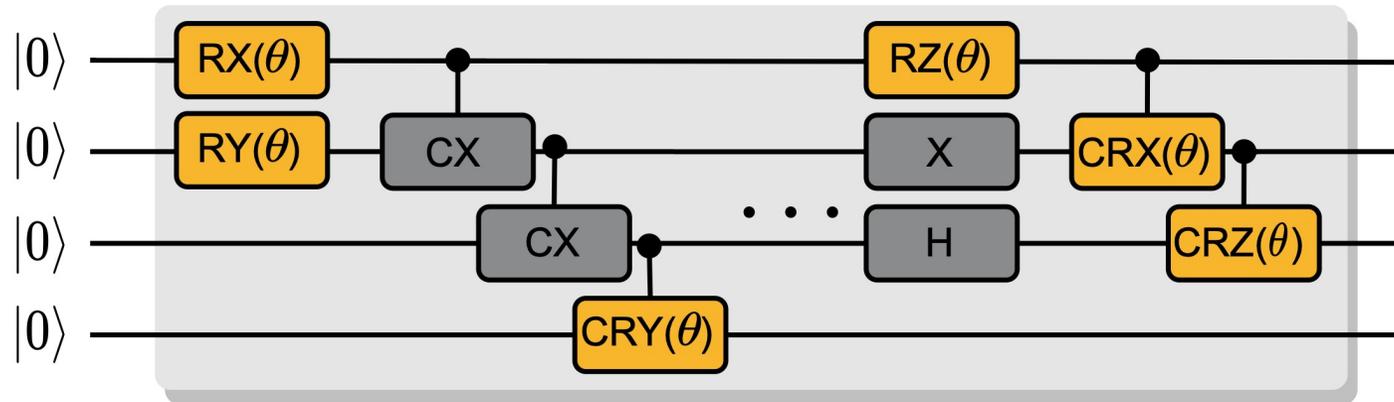
# Parameterized Quantum Circuits (PQC)

- Parameterized Quantum Circuits (PQC)
- Quantum circuit with fixed gates and **parameterized gates**



# Parameterized Quantum Circuits (PQC)

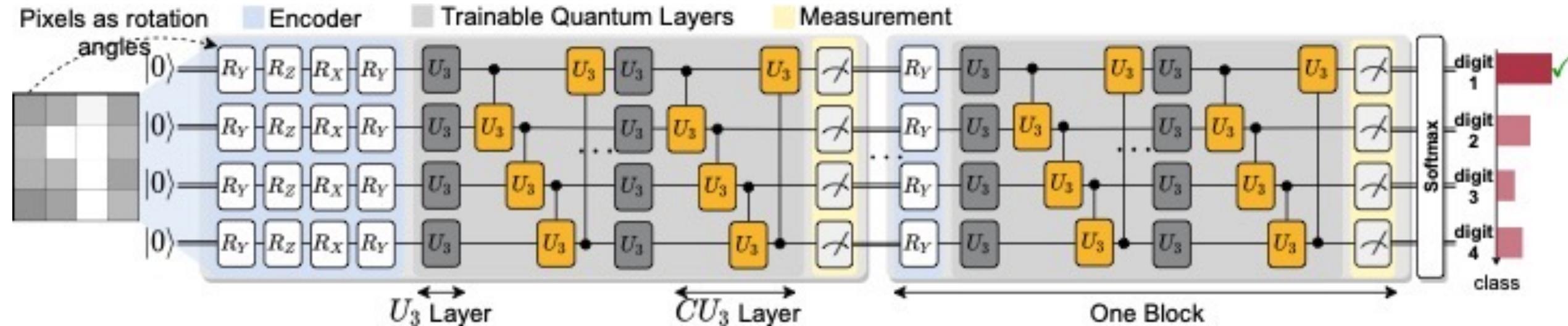
- Parameterized Quantum Circuits (PQC)
- Quantum circuit with fixed gates and **parameterized gates**



- PQCs are commonly used in **hybrid classical-quantum** models and show promises to achieve quantum advantage
  - Variational Quantum Eigensolver (VQE)
  - Quantum Neural Networks (QNN)
  - Quantum Approximate Optimization Algorithm (QAOA)

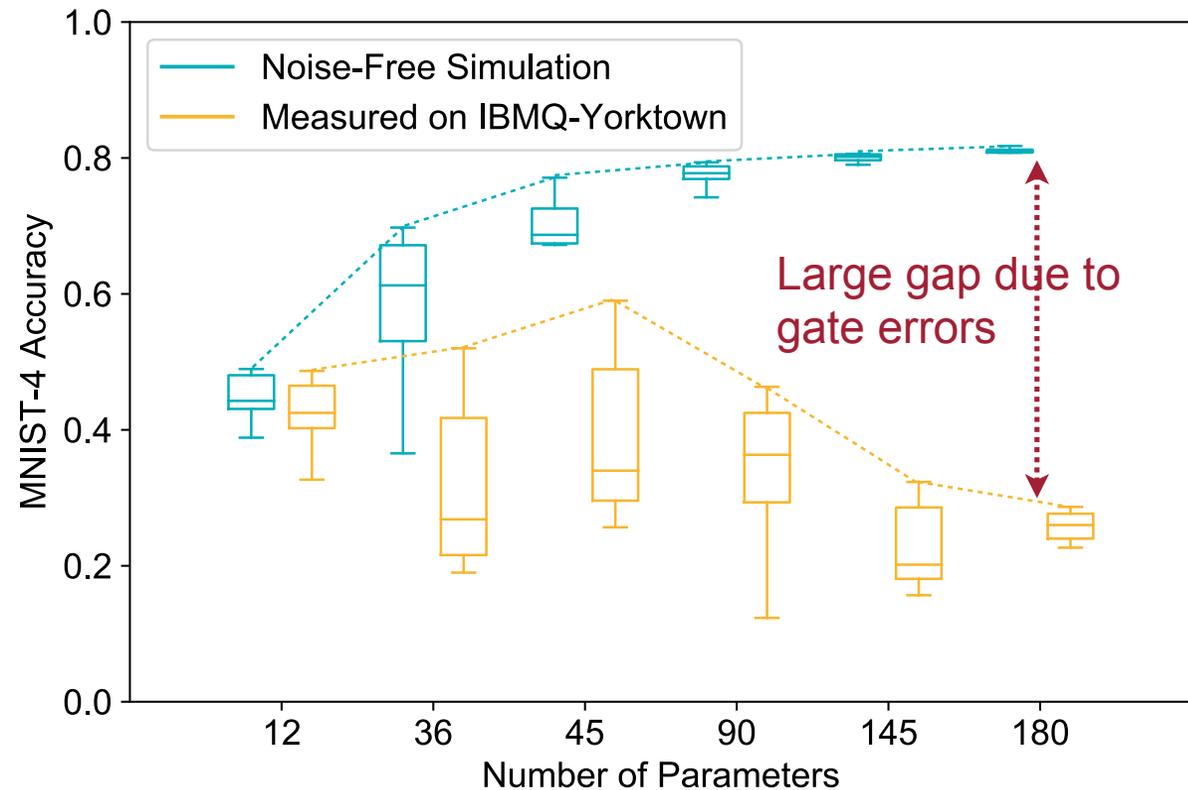
# Quantum Neural Networks (QNN)

- QNN is one kind of PQC for machine learning tasks
  - Encoder
  - Trainable Quantum Layers
  - Measurements



# Challenge of PQC: Noise

- Noise **degrades** the PQC reliability
  - Large **gap** between the noise-free simulation and real deployment

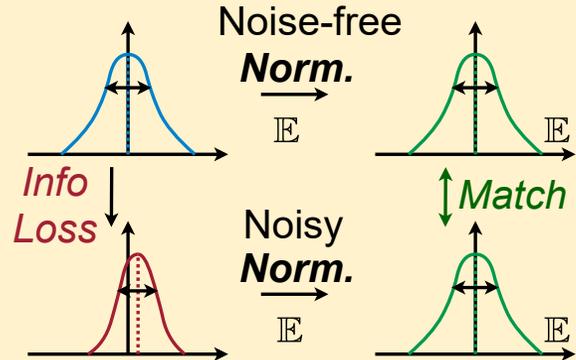


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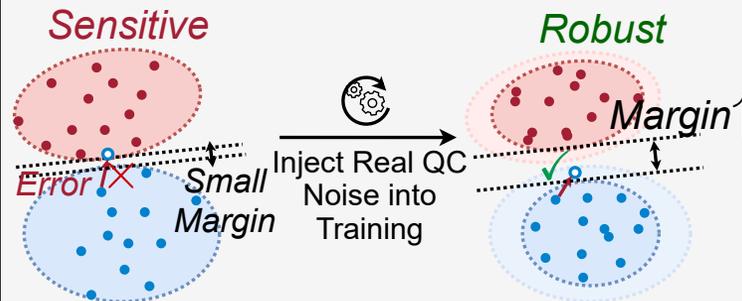
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# Three Techniques in QuantumNAT

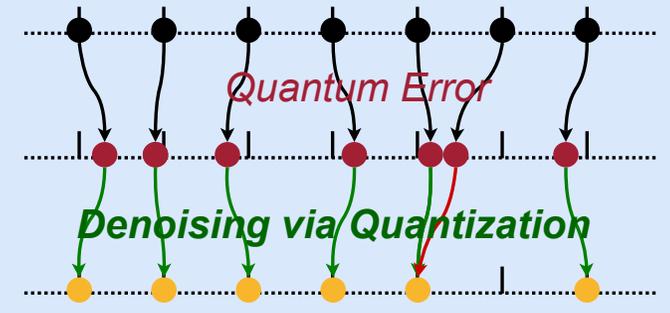
## (1) Post-Measurement Normalization



## (2) Real QC-backed Noise Injection

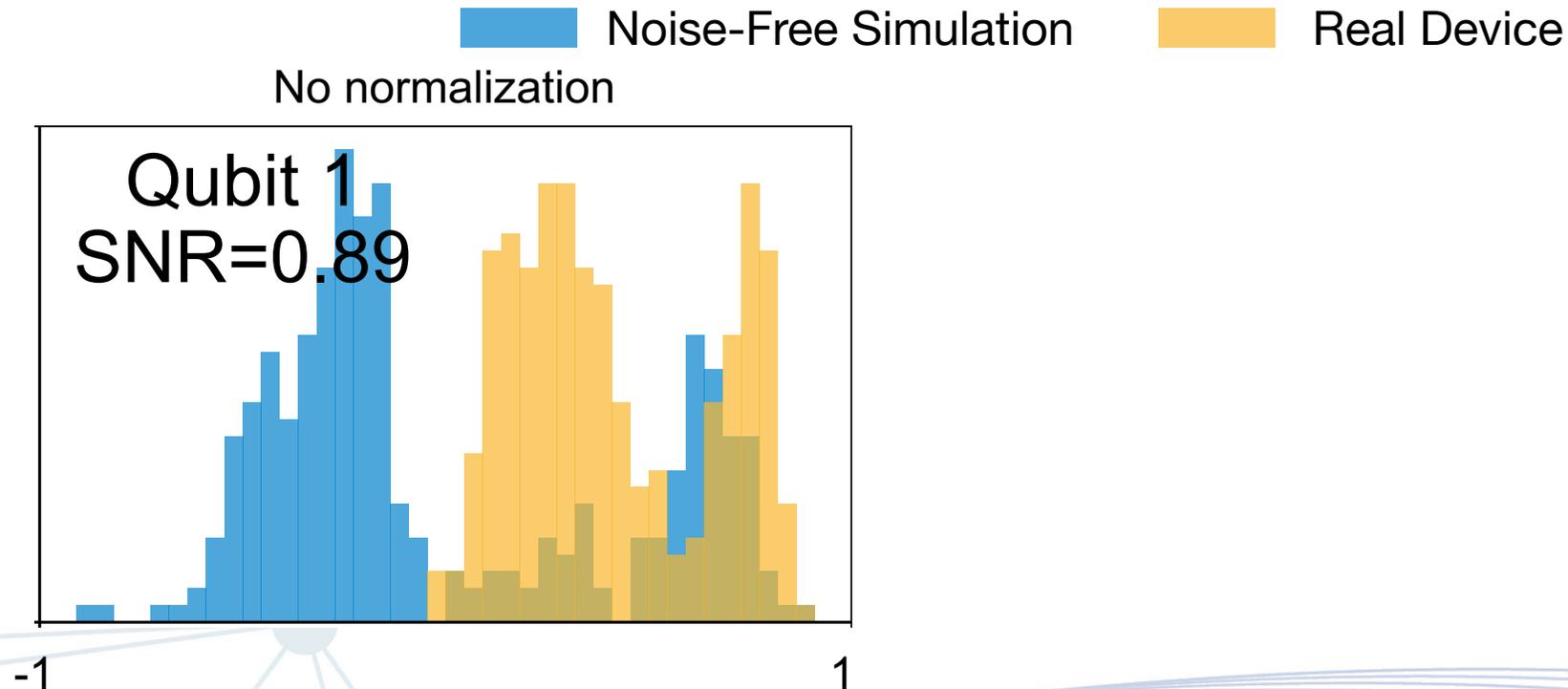


## (3) Post-Measurement Quantization



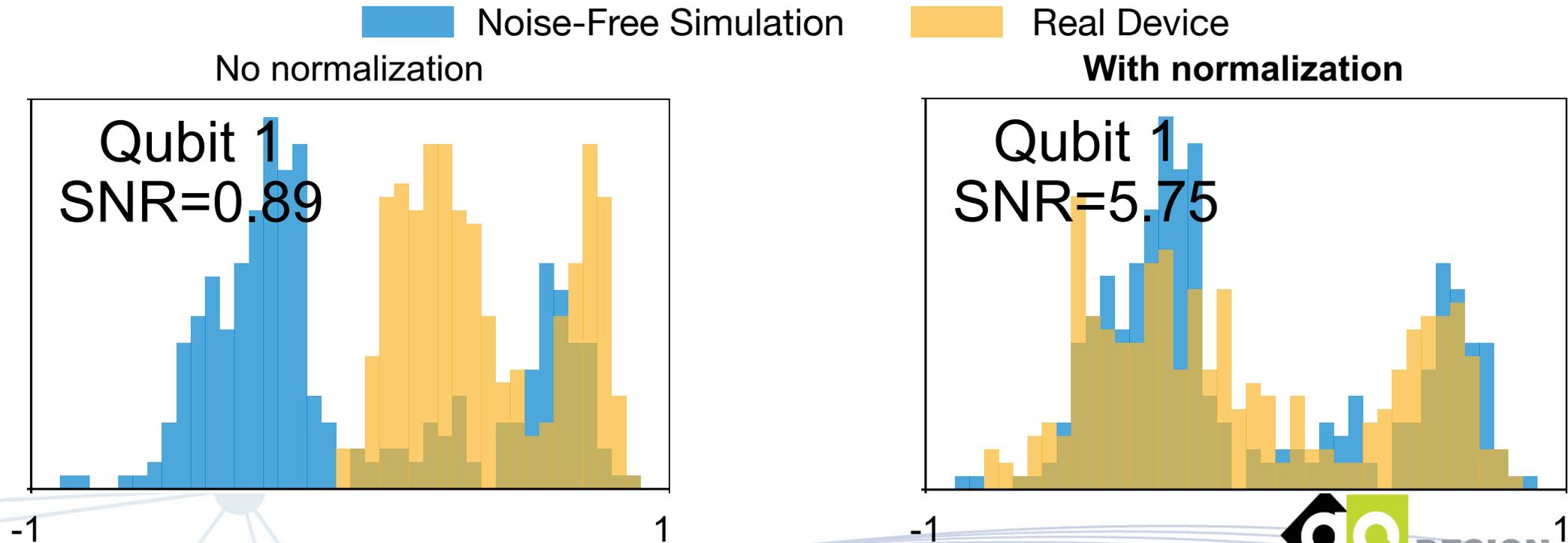
# Post-Measurement Normalization

- Normalize the measurement outcome (expectation value)
  - Along the **batch** dimension
- Measurement outcome distribution of 50 quantum circuits:



# Post-Measurement Normalization

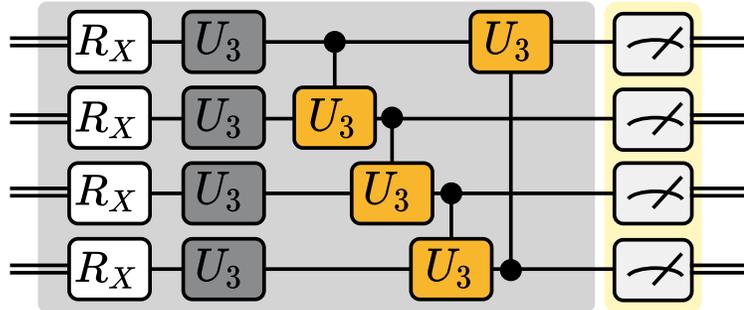
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# Noise Injection

- Inject noise during training on classical simulator
  - Pauli error
  - Readout error

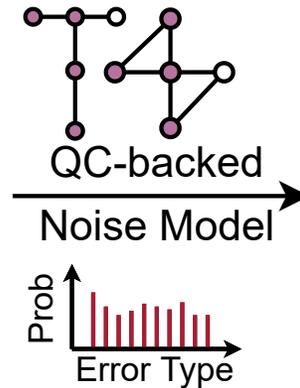
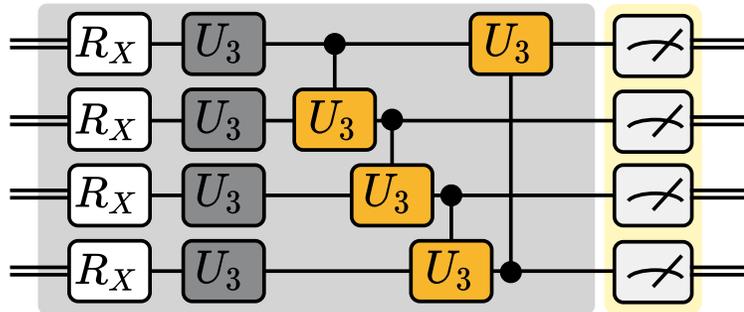
Compiled Quantum Circuits  
(Noise-free)



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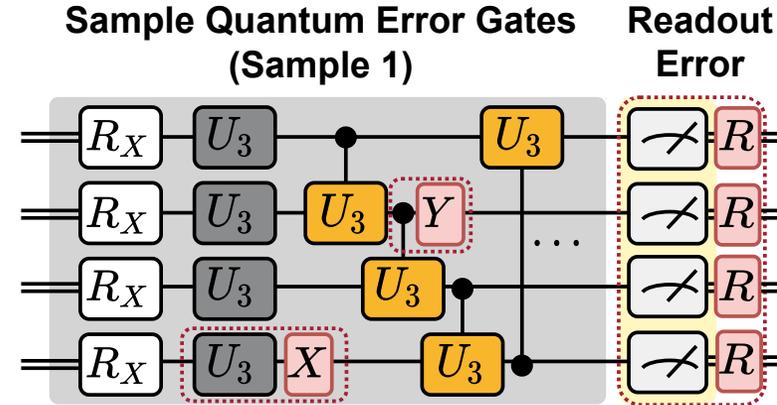
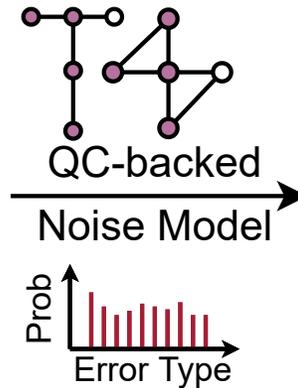
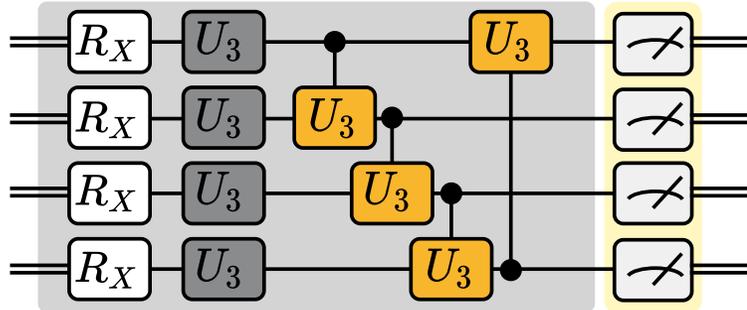
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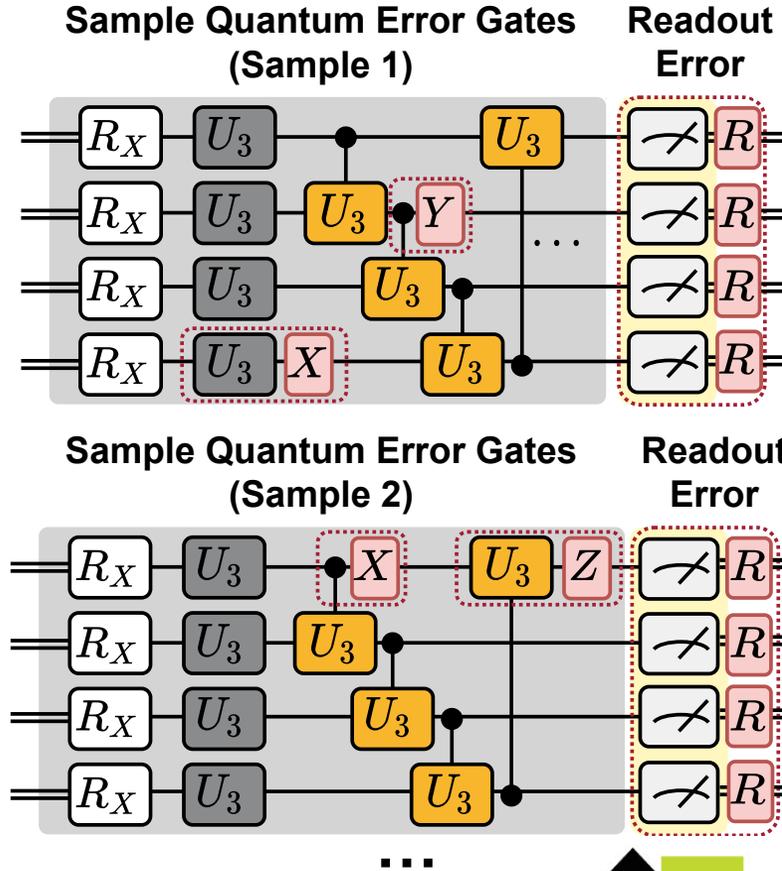
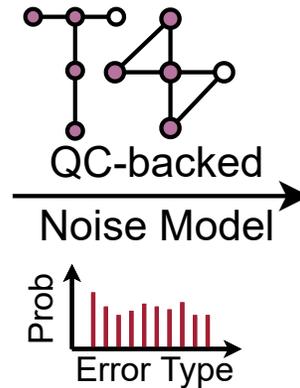
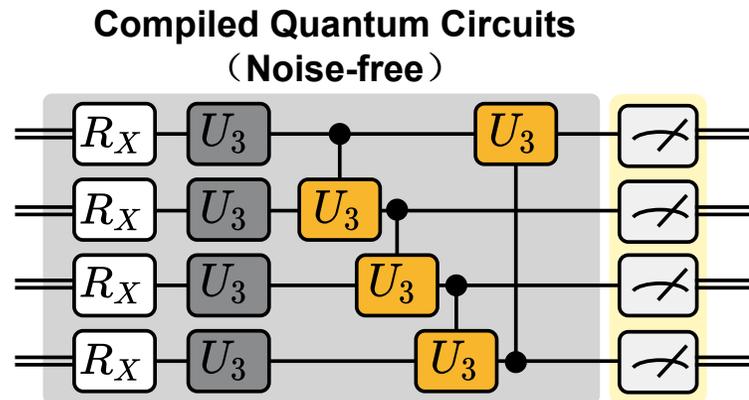
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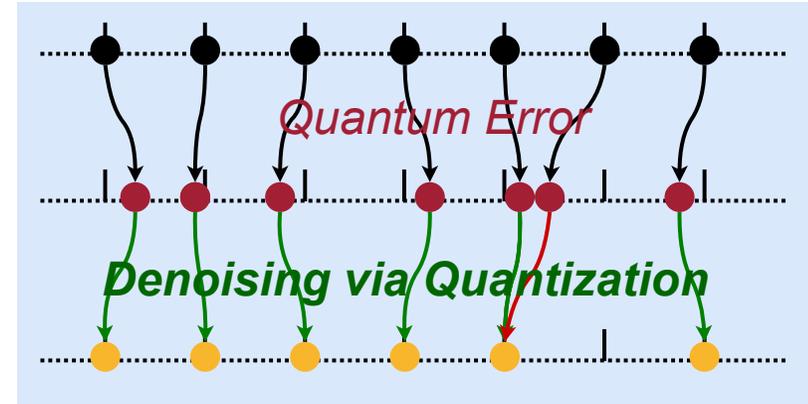
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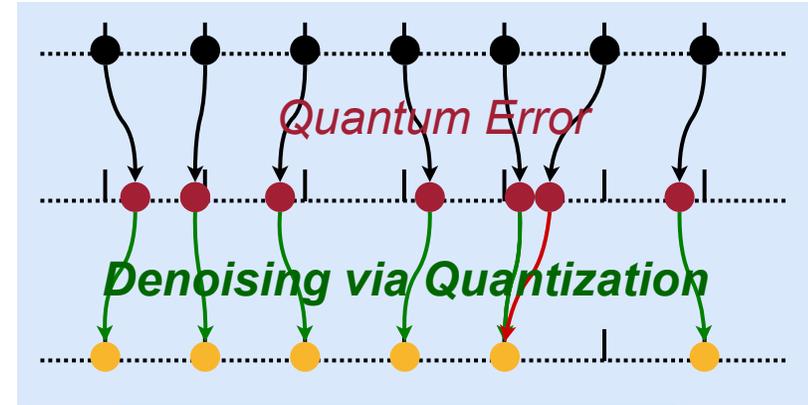
# Post-Measurement Quantization

- Quantize measurement outcomes (expectation values)
  - Denoising effect
  - Small errors will be mitigated

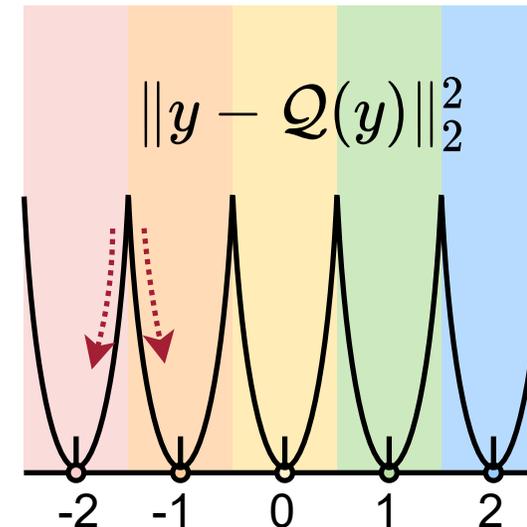


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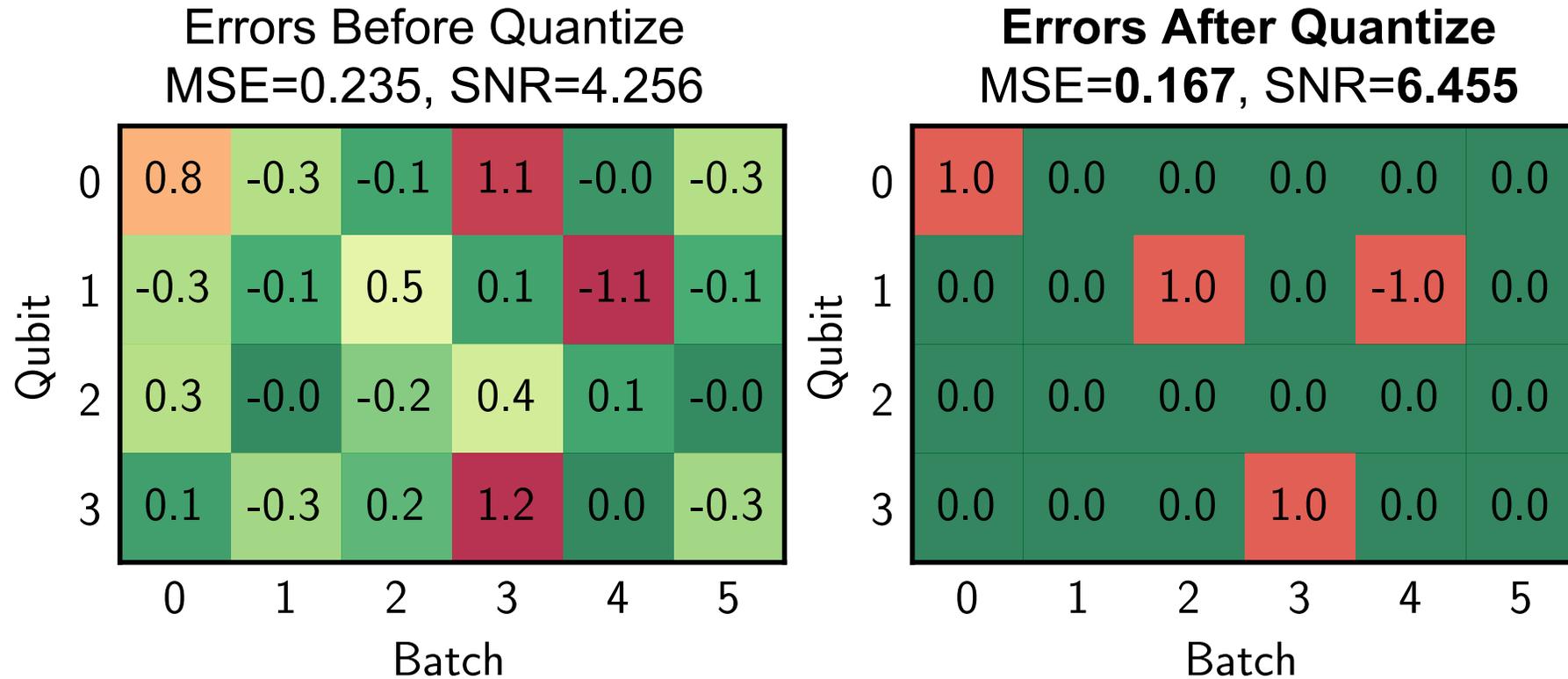


- **Loss** term to encourage measurement outcomes to be close to **centroids**



# Post-Measurement Quantization

- Quantization reduces errors and improves SNR



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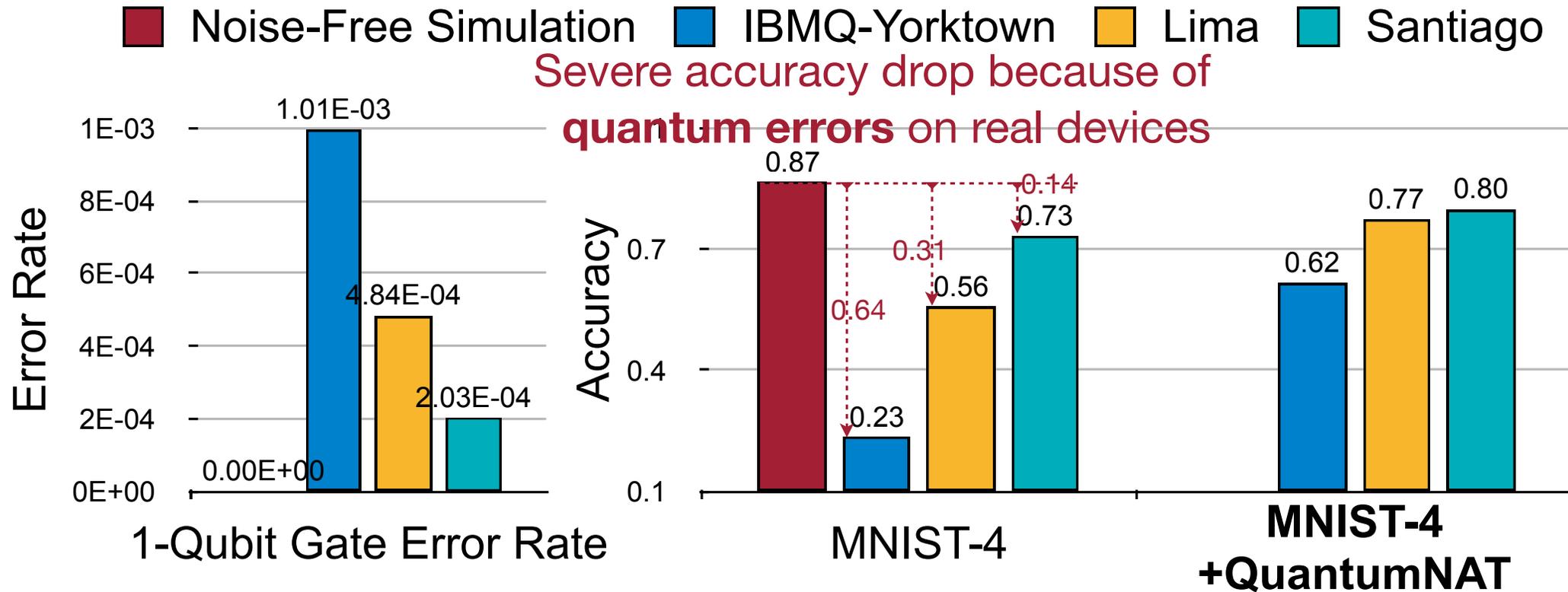
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# Evaluation

- Benchmarks
  - Quantum Machine Learning task: MNIST 10-class, 4-class, 2-class, Fashion MNIST 10-class, 4-class, 2-class, Vowel 4-class, Cifar-2 class
- Quantum Devices
  - IBMQ
  - #Qubits: 5 to 15
  - Quantum Volume: 8 to 32

# Evaluation

- QuantumNAT significantly improves real measurement accuracy



# Consistent Improvements on Various Benchmarks

- Different quantum devices
- Different models
- Different tasks

Model	Method	MNIST-4	Fash.-4	Vow.-4	MNIST-2	Fash.-2	Cifar-2
2B×12L Santiago	Baseline	0.30	0.32	0.28	0.84	0.78	0.51
	+ Post Norm.	0.41	0.61	0.29	0.87	0.68	0.56
	+ Gate Insert.	0.61	0.70	0.44	0.93	0.86	0.57
	+ Post Quant.	<b>0.68</b>	<b>0.75</b>	<b>0.48</b>	<b>0.94</b>	<b>0.88</b>	<b>0.59</b>
2B×2L Yorktown	Baseline	0.43	0.56	0.25	0.68	0.70	0.52
	+ Post Norm.	0.57	0.60	0.38	0.86	0.72	0.56
	+ Gate Insert.	0.58	0.60	<b>0.45</b>	0.91	0.85	0.57
	+ Post Quant.	<b>0.62</b>	<b>0.65</b>	0.44	<b>0.93</b>	<b>0.86</b>	<b>0.60</b>
2B×6L Belem	Baseline	0.28	0.26	0.20	0.46	0.52	0.50
	+ Post Norm.	0.52	0.57	0.33	0.81	0.62	0.51
	+ Gate Insert.	0.52	0.60	0.37	0.84	<b>0.82</b>	0.57
	+ Post Quant.	<b>0.58</b>	<b>0.62</b>	<b>0.41</b>	<b>0.88</b>	0.80	<b>0.61</b>
3B×10L Athens	Baseline	0.29	0.36	0.21	0.54	0.46	0.49
	+ Post Norm.	0.44	0.46	0.37	0.51	0.51	0.50
	+ Gate Insert.	-	-	-	-	-	-
	+ Post Quant.	<b>0.56</b>	<b>0.64</b>	<b>0.41</b>	<b>0.87</b>	<b>0.64</b>	<b>0.53</b>
Model	Method	MNIST-10	Fash.-10	Avg.-All			
2B×2L Melbo.	Baseline	0.11	0.09	0.42			
	+ Post Norm.	0.08	0.12	0.52			
	+ Gate Insert.	0.25	0.24	0.61			
	+ Post Quant.	<b>0.34</b>	<b>0.31</b>	<b>0.64</b>			

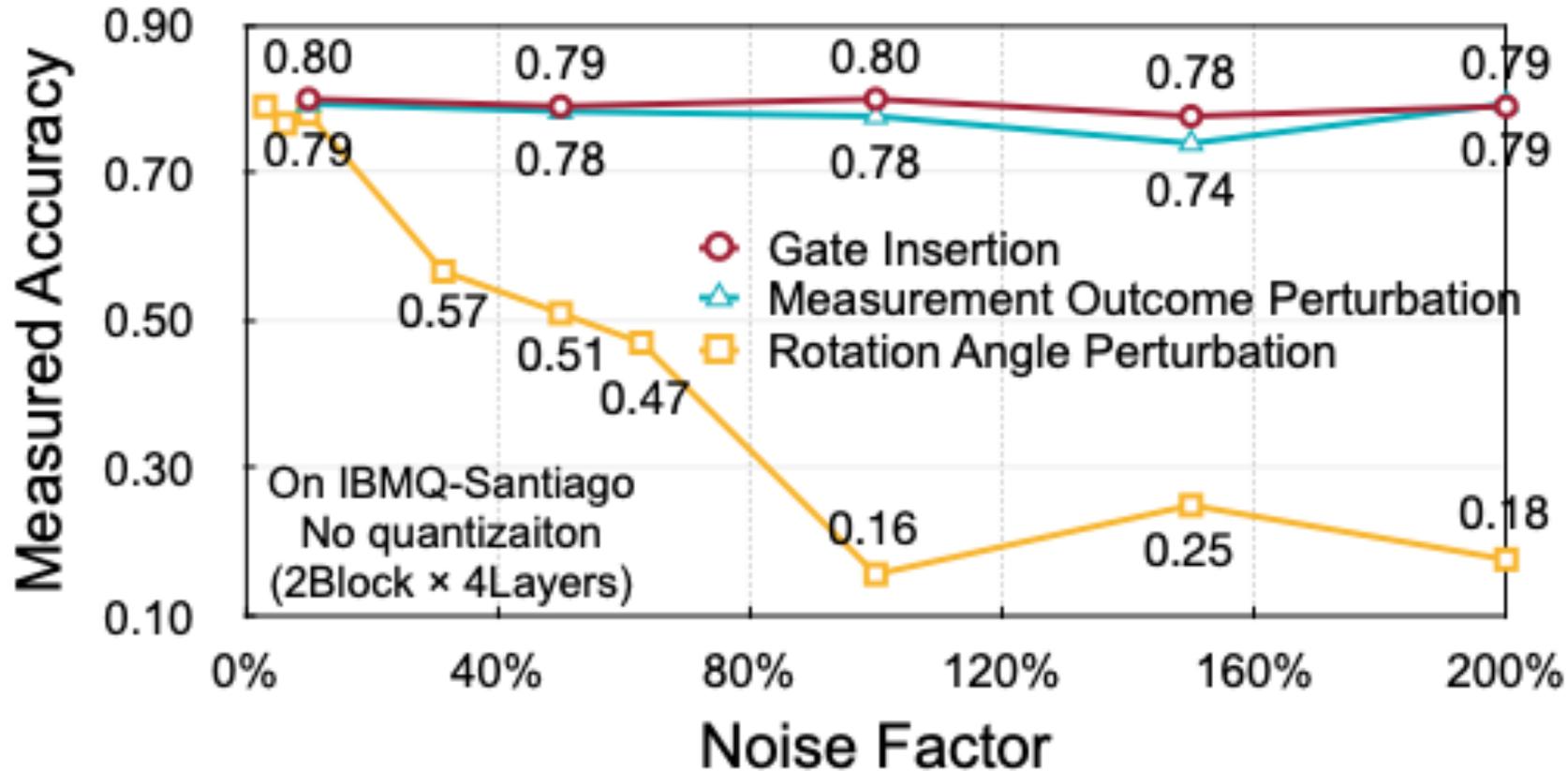
# Consistent Improvements on Various Benchmarks

- Different gate set design spaces

Design Space	MNIST-4		Fashion-2	
	Yorktown	Santiago	Yorktown	Santiago
'ZZ+RY'	<b>0.43</b>	0.57	0.80	<b>0.91</b>
<b>+QuantumNAT</b>	0.34	<b>0.60</b>	<b>0.83</b>	0.86
'RXYZ'	0.57	0.61	0.88	0.89
<b>+QuantumNAT</b>	<b>0.61</b>	<b>0.70</b>	<b>0.92</b>	<b>0.91</b>
'ZX+XX'	0.29	0.51	<b>0.52</b>	0.61
<b>+QuantumNAT</b>	<b>0.38</b>	<b>0.64</b>	<b>0.52</b>	<b>0.89</b>
'RXYZ+U1+CU3'	0.28	<b>0.25</b>	0.48	0.50
<b>+QuantumNAT</b>	<b>0.33</b>	0.21	<b>0.53</b>	<b>0.52</b>

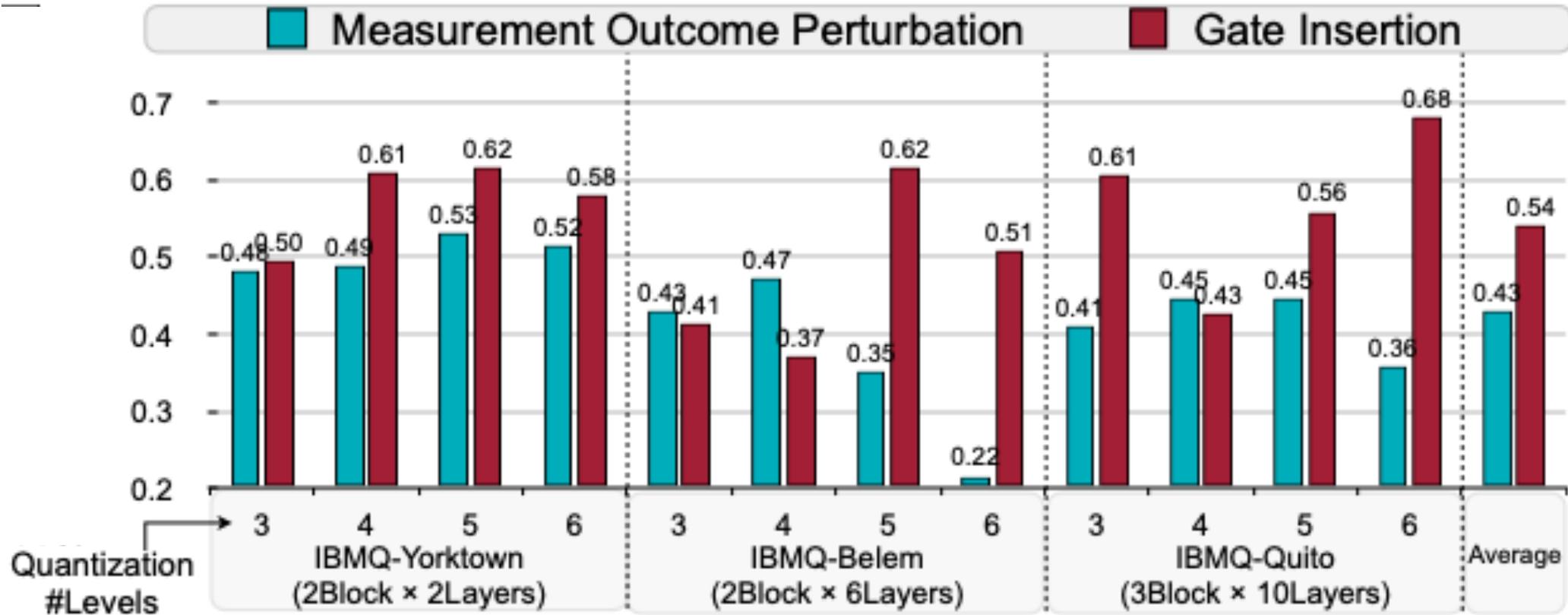
# Ablation Study on Noise Injection Method

- Gate insertion is better than rotation angle perturbation



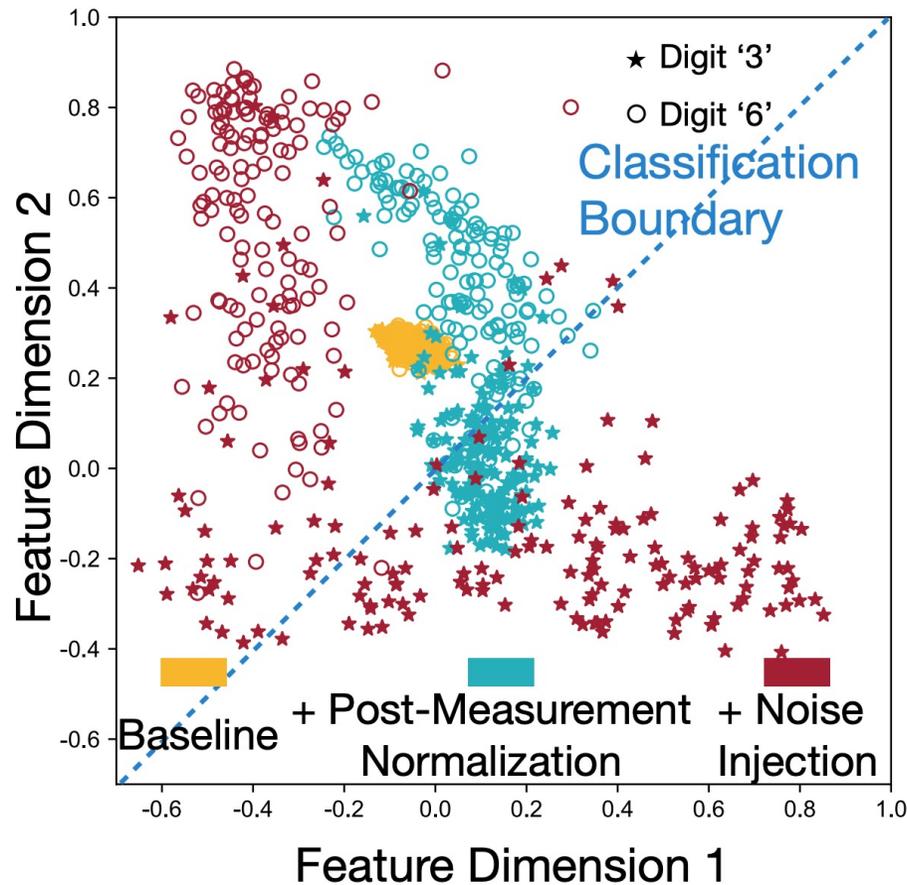
# Ablation Study on Noise Injection Method

- Gate insertion is better than measurement outcome perturbation



# Visualization

- QuantumNAT stretches the distribution of features
  - MNIST-2 classification task



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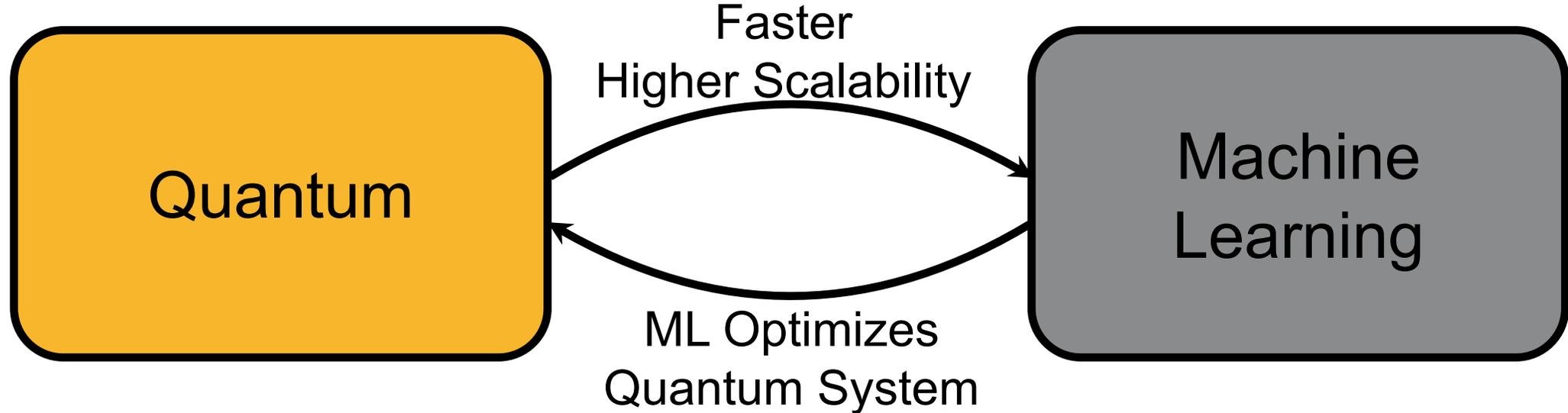
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Torch  
Quantum

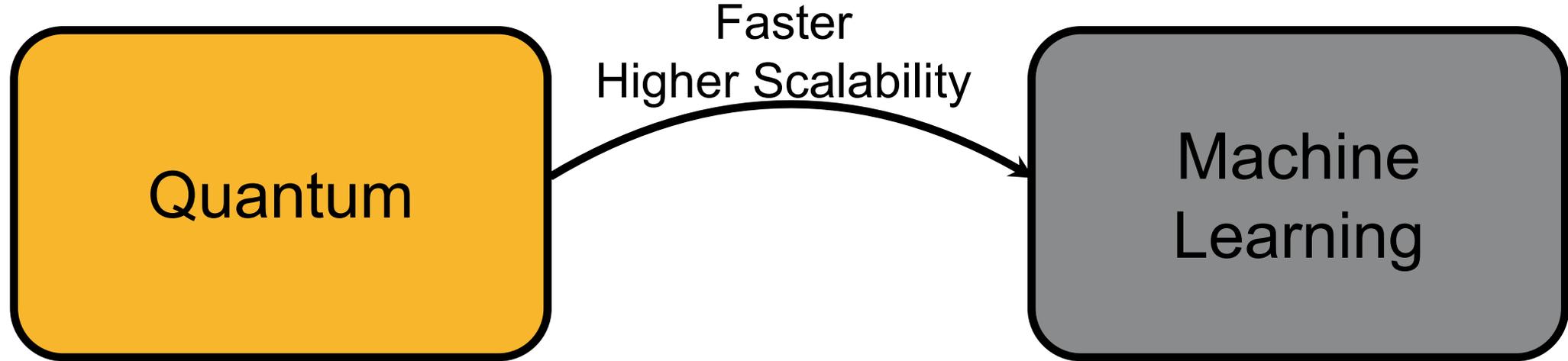
# Open-source: TorchQuantum

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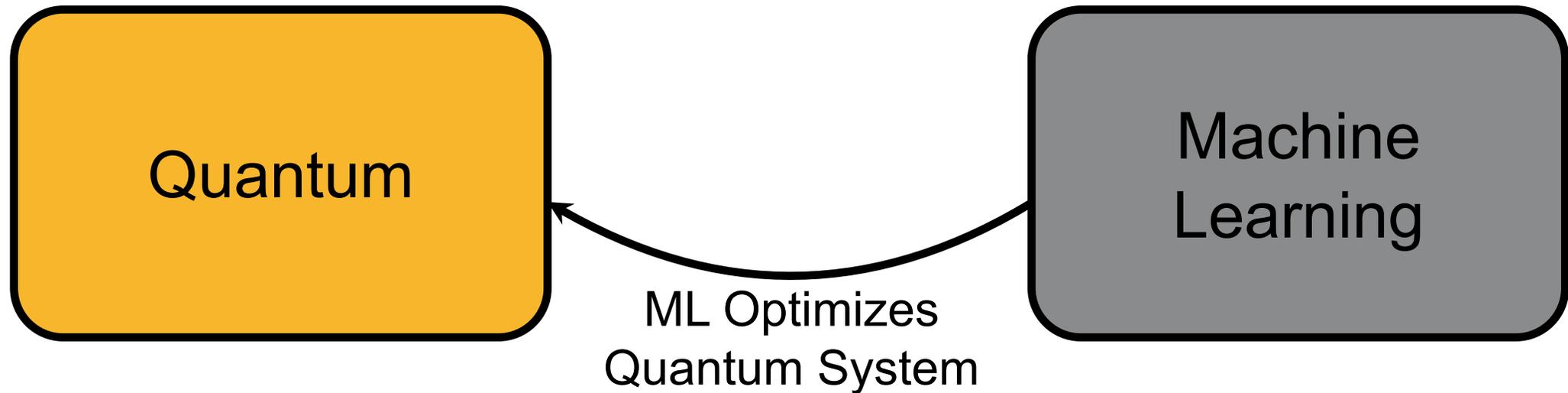
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- Quantum ML
  - Quantum neural networks
  - Quantum kernel methods

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- ML for Quantum
  - ML optimizes quantum compilation

# TorchQuantum Features

- Features
  - Easy construction of **parameterized quantum circuits** such as Quantum Neural Networks in PyTorch
  - Support **batch mode inference and training** on GPU/CPU, supports highly-parallelized training
  - Support **easy deployment** on real quantum devices such as IBMQ
  - Provide tutorials, videos and example projects of QML and using ML to optimize quantum computer system problems

# TorchQuantum Examples & Tutorials



## TorchQuantum Tutorials Opening

Hanrui Wang  
MIT HAN Lab



## TorchQuantum Tutorials Quantum Evolutional Neural Network

Zirui Li, Hanrui Wang  
MIT HAN Lab



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# Conclusion

- QuantumNAT: makes PQC **parameters** more noise-robust
  - Post-measurement Normalization
  - Noise injection
  - Post-measurement Quantization
- Achieve 94% 2-class and 34% 10-class classification accuracy
- Open-sourced **TorchQuantum** library for Quantum + ML research



<https://github.com/mit-han-lab/torchquantum>



[qmlsys.mit.edu](http://qmlsys.mit.edu)

